

# Analysis and Control of Multi-Agent Systems

#### Daniel Zelazo

Faculty of Aerospace Engineering Technion-Israel Institute of Technology



### Organizational Matters

#### **Instructor and Office Hours**

Daniel Zelazo - dzelazo@technion.ac.il

Room: Pfaffenwaldring 9 Room: 1.103

office hrs: Wed. 14:00 -16:00 (or by appointment)

#### **Teaching Assistant**

Jan Maximilian Montenbruck jan-maximilian.montenbruck@ist.uni-stuttgart.de

#### **Course Web-Page**

http://www.ist.uni-stuttgart.de/education/courses/Multi-Agent2014/

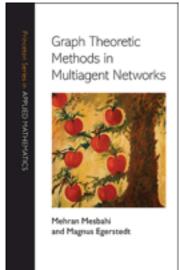
#### **Schedule**

Please see website for latest information!



### Organizational Matters

#### (suggested) Text Book



"Graph Theoretic Methods in Multiagent Networks" Mehran Mesbahi & Magnus Egerstedt Princeton University Press, 2010.

http://press.princeton.edu/titles/9230.html

**Homeworks:** - There will be a series of *optional* exercises that will accompany every few lectures. It is encouraged that you try to work through these.

Final Exam (July 23, 15:00-16:30): - A comprehensive written exam.

Multi-Agent Systems are systems composed of multiple interacting dynamic units.

biologically inspired...

shimmering of giant honeybees Kastberger G, Schmelzer E, Kranner I (2008) Social Waves in Giant Honeybees Repel Hornets. PLoS ONE 3(9): e3141.



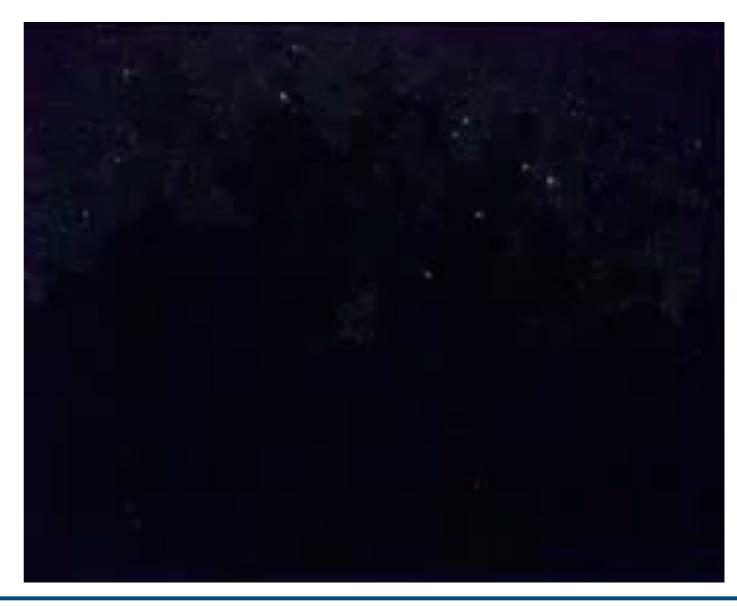


Multi-Agent Systems are systems composed of multiple interacting dynamic units.

biologically inspired...

#### synchronizing fireflies

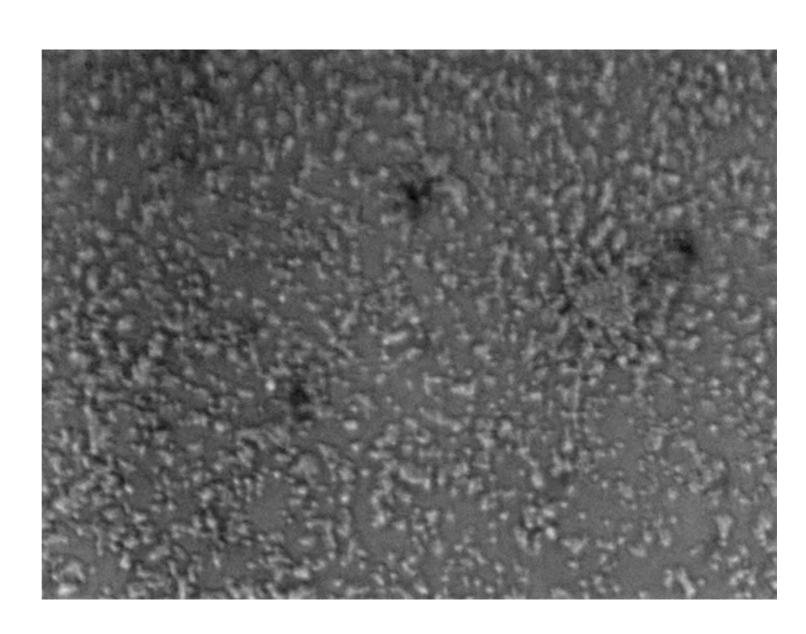
Buck, J and Buck, E (1968) Mechanism of Rhythmic Synchronous Flashing of Fireflies. Science 22 159(3821):1319-1327.





Multi-Agent Systems are systems composed of multiple interacting dynamic units.

biologically inspired...



**Aggregation of Dictyostelium** Goldbeter, Bulletin of Mathematical Biology 2006



Multi-Agent Systems are systems composed of multiple interacting dynamic units.

#### **Synchronization**

An agreement by multiple systems on a common state

#### **Coordination**

Managing of multiple interacting systems to achieve a team objective



#### Course Goals

#### **Course Goals**

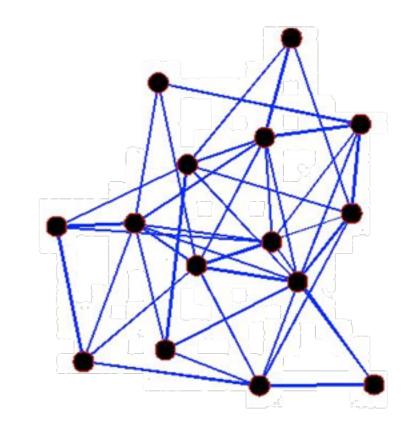
- Modeling of multi-agent systems
  - dynamics
  - interconnections
- Analysis of multi-agent systems
  - stability and performance
  - convergence
- •Synthesis of multi-agent systems
  - control
  - interconnection design
- Applications of multi-agent systems
  - formations

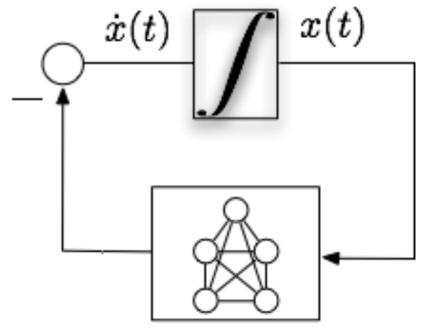


#### Course Goals

#### **Course Goals**

- Graph Theory
  - combinatorics
  - algebraic graph theory
- Consensus and Agreement Protocols
  - continuous and discrete systems
  - undirected/directed communication
  - linear and non-linear systems, switched systems
- Networks as Systems
  - graph theory ←→ systems theory



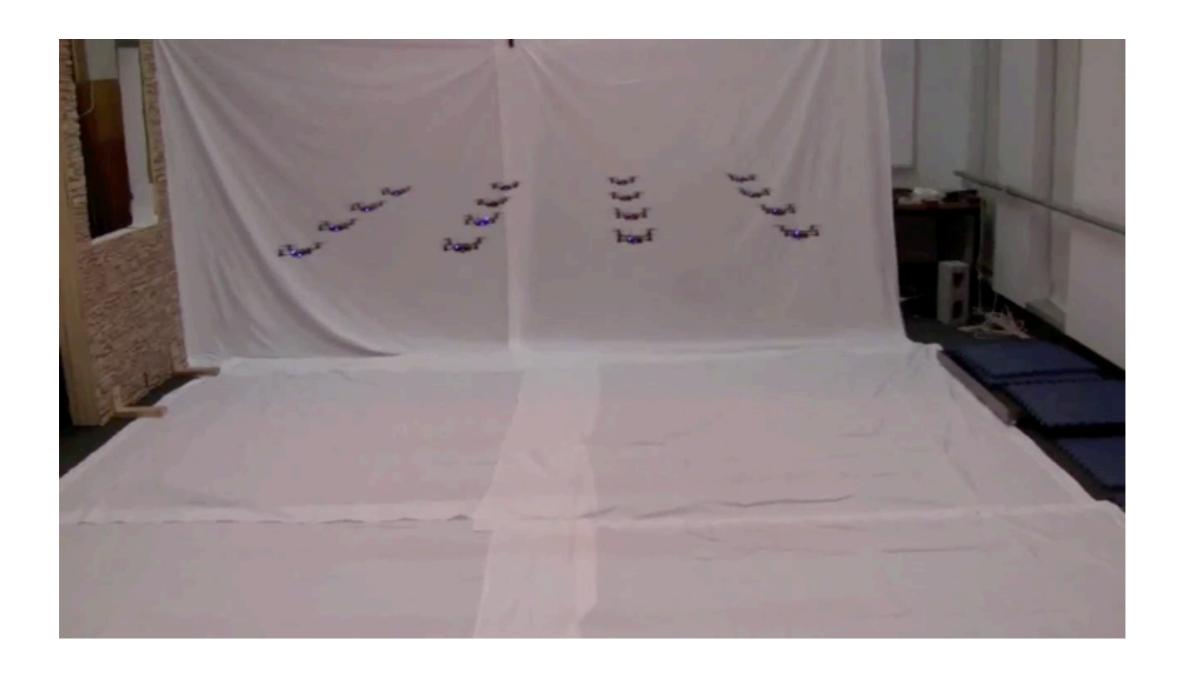


### Course Goals

#### **Course Schedule**

June 30 - July 23

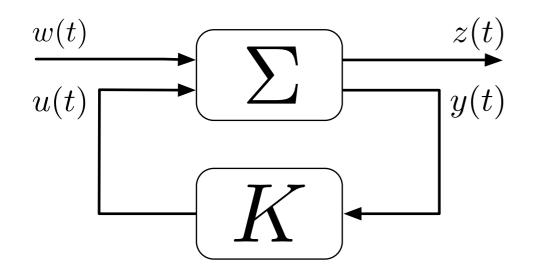
	Montag	Dienstag	Mittwoch	Donnerstag	Freitag
Week 1	- Introduction to MAS - Graph Theory	- Linear Consensus I - Gradient Systems	No Class	- Linear Consensus II	- Control of Networks
Week 2	- Performance of Networks	- Design of Networks	No Class	- Formation Control I	<ul><li>Formation Control II</li><li>Conclusions and Outlook</li></ul>
Week 3	No Class				
Week 4	No Class	No Class	Final Exam 15:00 - 16:30	No Class	No Class







$$\dot{x}_1(t) = f(x_1(t), u_1(t), t)$$



trajectory tracking robust control optimal estimation

optimal control nonlinear control model predictive control

linear non-linear CT, DT hybrid stochastic

• • •





$$\dot{x}_1(t) = f(x_1(t), u_1(t), t)$$



$$\dot{x}_2(t) = f(x_2(t), u_2(t), t)$$



$$\dot{x}_3(t) = f(x_3(t), u_3(t), t)$$





$$\dot{x}_1(t) = f_1(x_1(t), u_1(t), t)$$

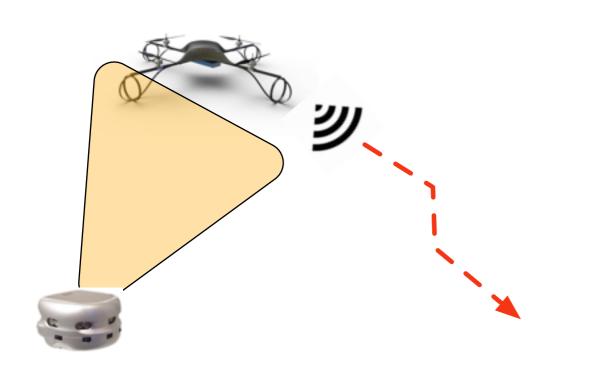


$$\dot{x}_2(t) = f_2(x_2(t), u_2(t), t)$$



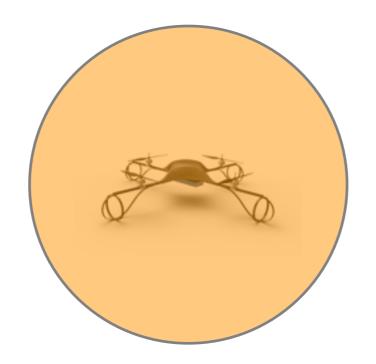
$$\dot{x}_3(t) = f_1(x_3(t), u_3(t), t)$$





omnidirectional
vision
radar
relative sensing
range measurements

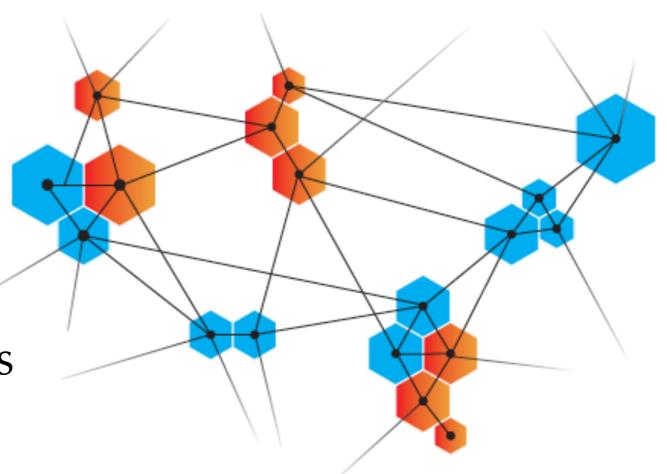
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### Networked Dynamic Systems

### Why is this hard?

- large-scale
- complexity & scalability
- variety of interconnections
- •delays, bandwidth, etc...



# We need a new and dedicated approach for studying these systems!



### Networked Dynamic Systems

